Primary Mathematics Study on Whole Numbers

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ICMI Study 23





THE NUMBER LINE: A "WESTERN" TEACHING AID

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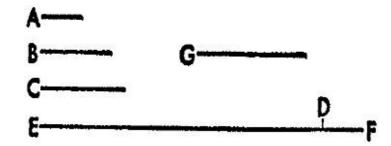
Didactical Phenomenology of Mathematical Structures (1999)

Modern textbooks start measuring much earlier than tradition allows, but unfortunately this kind of measuring is not yet sufficiently integrated with the operations on natural numbers.

The device beyond praise that visualises magnitudes and at the same time the natural numbers articulating them is the number line, where initially only the natural numbers are individualised and named (p.101).

Euclid

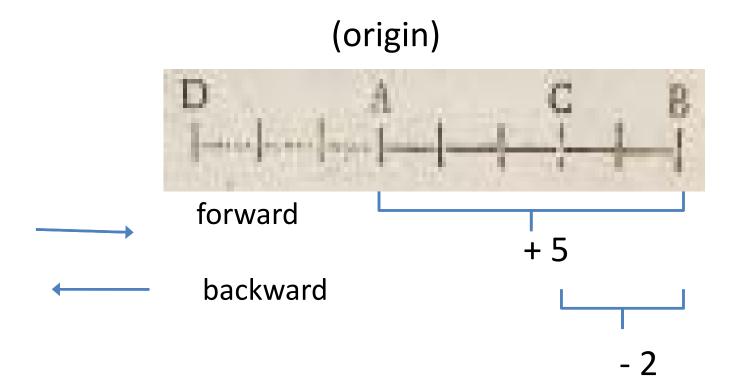
Magnitudes are represented by straight lines For instance: *Prime numbers are more than*



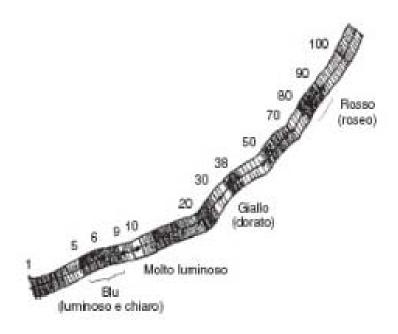
The line functions as a variable because nothing is known about the real size of the number it represent (R. Netz, 1999)

John Wallis (1685)

The first number line with unit marks dates back to John Wallis



Mental number line



There are neurocognitive studies on the evidence of a mental number line, but the universality of mental number line is controversial.

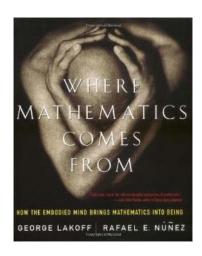
The conceptual metaphor of number line (embodied cognition)

Projection from a domain

(the spatial experience of motion along a path)
to another domain

(the arithmetic of whole numbers).

Very recent findings show that number processing is influenced by body movements.



Many didactical examples in Western countries: Hopping to construct the multiples of five



A long history Possible advantages why not in China?